

St John's Church of England Primary School

Maths and Calculation Policy

Date Approved:	Spring 2024	
Headteacher:	Miss Anna Pyatt	
Chair of Governors:	Mr Robin Davis	
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Love, Respect, Value

St John's Church of England Primary School is committed to high expectations for all and to embracing equality.

Our Vision:

Through 'Growing Together in Love and Respect', we provide the opportunity for every child to reach their full potential. We embrace Christian values and ensure all children are ready for their next steps in a learning environment that provides a balance between skills, knowledge, learning from and embracing mistakes and mastery approach.

Rationale

Mathematics equips pupils with a uniquely powerful set of tools to understand and change the world. These tools include logical reasoning, problem solving skills and the ability to think in abstract ways.

Mathematics is important in everyday life. It is integral to all aspects of life and with this in mind we endeavour to ensure that children develop a positive and enthusiastic attitude towards mathematics that will stay with them.

The National Curriculum for mathematics describes in detail what pupils must learn in each year group. Combined with our Calculation Policy, this ensures continuity and progression and high expectations for attainment in mathematics.

It is vital that a positive attitude towards mathematics is encouraged amongst all of our pupils in order to foster confidence and achievement in a skill that is essential in our society. At St John's we use the Early years foundation stage statutory framework (2023) and the National Curriculum for Mathematics (2014) as the basis of our mathematics programme. Teachers use HfL Essentials Maths to support lesson-planning which is tailored to each class's needs.. We aim for all pupils to achieve mastery in the key concepts of mathematics, appropriate for their age group, in order that they make genuine progress and avoid gaps in their understanding that provide barriers to learning as they move through education. Assessment for Learning, an emphasis on investigation, problem solving and the development of mathematical thinking and a rigorous approach to the development of teacher subject knowledge are therefore essential components to successful mathematics at St John's school.

The calculation part of the policy outlines a model progression through written strategies for addition, subtraction, multiplication and division. Through the policy, we aim to link concrete manipulatives and representations in order that the children can be vertically accelerated through each strand of calculation. We know that school wide policies, such as this, can ensure consistency of approach, enabling children to progress stage by stage through models and representations they recognise from previous teaching, allowing for deeper conceptual understanding and fluency. Teachers will be presenting strategies and equipment appropriate to children in each class will be working at age-appropriate levels as set out in the National Curriculum and in line with school policy.

Aims

We aim to provide the pupils with a mathematics curriculum and high quality teaching to produce individuals who are numerate, creative, independent, inquisitive, enquiring and confident. We also aim to provide a stimulating environment and adequate resources so that pupils can develop their mathematical skills to the full.

Our pupils should:

- have a well-developed sense of the size of a number and where it fits into the number system
- know by heart number facts such as number bonds, multiplication tables, doubles and halves
- use what they know by heart to figure out numbers mentally
- calculate accurately and efficiently, both mentally and in writing and paper,
- drawing on a range of calculation strategies
- recognise when it is appropriate to use a calculator and be able to do so effectively
- make sense of number problems, including non-routine/'real' problems and identify the operations needed to solve them
- explain their methods and reasoning, using correct mathematical terms

- judge whether their answers are reasonable and have strategies for checking them where necessary
- suggest suitable units for measuring and make sensible estimates of measurements
- collect data and select methods to present appropriately
- explain and make predictions from the numbers in graphs, diagrams, charts and tables
- develop spatial awareness and an understanding of the properties of 2d and 3d shapes

Provision

Pupils are provided with a variety of opportunities to develop and extend their Mathematical skills, including:

- Group work
- Paired work
- Whole class teaching
- Individual work including 1:1 feedback

Pupils engage in:

- the development of mental strategies
- written methods
- practical work
- investigational work
- problem solving
- mathematical discussion
- consolidation of basic skills and number facts
- maths games

Maths Mastery

This approach of teaching emphasises a deep understanding of mathematical concepts, instead of accelerating through older year group curricula. Rooted in research-backed methodologies, Maths Mastery seeks to ensure that every student develops a solid foundation in mathematical principles before progressing to more advanced topics. By fostering a deeper understanding of mathematical concepts, Maths Mastery aims to equip students with the tools needed for lifelong mathematical success, laying the groundwork for a more confident and proficient approach to future mathematical challenges.

Concrete, Pictorial, Abstract (CPA)

Teaching for mastery can be broken down into three distinct stages. In the concrete stage, pupils engage with tangible, hands-on materials to physically manipulate and experience mathematical ideas. This experience helps build a solid foundation of understanding. The pictorial stage follows, where pupils transition from physical objects to visual representations, such as diagrams or drawings, allowing them to connect the concrete experiences with more symbolic representations. The third stage is the abstract stage, where pupils work with numerical and symbolic representations such as mathematical symbols and equations, applying the conceptual understanding gained through the concrete and pictorial stages. The CPA approach acknowledges the diverse learning styles of students and aims to provide a well-rounded, multi-sensory learning experience that fosters deep comprehension and mastery of mathematical concepts.

We recognise the importance of establishing a secure foundation in mental calculation and recall of number facts before standard written methods are introduced. We use accurate mathematical vocabulary in our teaching and children are expected to use it in their verbal and written explanations.

Mathematics contributes to many subjects and it is important that children are given opportunities to apply and use Mathematics in real contexts. It is important that time is found in other subjects for pupils to develop their numeracy skills, e.g. there should be regular, carefully planned opportunities for measuring in science and technology, for the consideration of properties of shape and geometric patterns in technology and art, and for the collection and presentation of data in science, history and geography. We endeavour at all times to set work that is challenging, motivating and encourages the pupils to think about how they learn and to talk about what they have been learning. Additional enrichment opportunities are provided for pupils to further develop mathematical thinking e.g. through cooking, music, and maths investigations and games.

Teachers plan problem solving and investigational activities throughout each unit to ensure that pupils develop the skills of mathematical thinking and enquiry.

To provide adequate time for developing mathematics, maths is taught daily and discretely. Maths lessons may vary in length but will usually last for about 30 minutes in Early Years Foundation Stage, 50 minutes in Key Stage 1 and 60 minutes in Key Stage 2.

Teaching Approaches

Teachers use a range of teaching strategies to engage the children in maths and ensure progress is made by all children within a class; no set formula is used. A typical lesson would include:

- Both teaching input and pupil activities,
- A balance between whole class, guided grouped and independent work, (groups, pairs and individual work)
- effectively scaffolded and opportunities for children to explore appropriate challenging activities.

Sometimes the focus for the session is new learning, at other times pupils may be practising, to master the application of a concept they have learned earlier. The focus of the session may vary for different children depending on their learning needs.

At times there may be opportunities to develop skills and understanding of mathematics through additional activities, some of which may take place at home.

Assessment

Formative Assessment

Teachers integrate the use of formative assessment strategies such as effective questioning, clear learning objectives, the use of success criteria and effective feedback and response in their teaching.

Summative Assessment

Using termly assessments, pupils are assessed against Age Related Expectations. The school's MIS progress tracking system is updated termly.

Statutory National Curriculum tests are used at the end of KS2; teachers use past questions and papers throughout the year as a part of the teaching and learning to inform their assessments as they prepare pupils for these assessments.

All assessments and teaching informs teachers' understanding of a child's attainment in maths and this is recorded on the school's MIS progress tracking system

The school's Assessment, Feedback and Reporting Policy informs high quality feedback and pupils' response to it in Mathematics.

Early Years Foundation Stage (EYFS)

We follow EYFS curriculum guidance for Mathematics. However, we are committed to ensuring the confident development of number sense and put emphasis on mastery of key early concepts. Pupils will explore numbers to 20 with a key focus on understanding to 10 and the development of models and images for numbers as a solid foundation for further progress. They will be able to develop subitising skills (instantly recognising small numbers of objects) as well as explore and represent patterns within numbers up to 10.

Resources

A bank of essential concrete mathematical resources including Numicon, Cuisenaire rods, bead strings, multi link cubes etc are available in every classroom to be used as day to day resources. Further resources supporting whole school requirements are kept in the Sky Floor (blue Level 2) resource cupboard.

Role of the Subject Leader

- Ensures teachers understand the requirements of the National Curriculum and helps them to plan lessons.
- Leads by example by setting high standards in their own teaching.
- Prepares, organises and leads CPD and joint professional development.
- Works with the SENCO.
- Observes colleagues from time to time with a view to identifying the support they need.
- Attends CPD and feeds back for whole school impact
- Keeps parents informed about Mathematics issues and promote parental engagement.
- Discusses regularly with the Headteacher and the governors the progress of whole school maths.
- Deploys support staff to address mathematics related needs within the school.
- Monitors and evaluates mathematics provision in the school by conducting regular work scrutiny, learning walks, pupil voice interviews and assessment data analysis.

The importance of mental mathematics

While this policy focuses on written calculations in mathematics, we recognise the importance of the mental strategies and known facts that form the basis of all calculations. The following checklists outline the key skills and number facts that children are expected to develop throughout the school.

To add and subtract successfully, children should be able to:

- recall all addition pairs to 9 + 9 and number bonds to 10
- · recognise addition and subtraction as inverse operations
- add mentally a series of one digit numbers (e.g. 5 + 8 + 4)
- add and subtract multiples of 10 or 100 using the related addition fact and their knowledge of place value (e.g. 600 + 700, 160 70)
- partition 2 and 3 digit numbers into multiples of 100, 10 and 1 in different ways (e.g. partition 74 into 70 + 4 or 60 + 14)
- · use estimation by rounding to check answers are reasonable

To multiply and divide successfully, children should be able to:

- · add and subtract accurately and efficiently
- · recall multiplication facts to $12 \times 12 = 144$ and division facts to $144 \div 12 = 12$
- use multiplication and division facts to estimate how many times one number divides into another etc.
- know the outcome of multiplying by 0 and by 1 and of dividing by 1
- understand the effect of multiplying and dividing whole numbers by 10, 100 and later 1000
- · recognise factor pairs of numbers (e.g. that $15 = 3 \times 5$, or that $40 = 10 \times 4$) and increasingly able to recognise common factors
- derive other results from multiplication and division facts and multiplication and division by 10 or 100 (and later 1000)
- · notice and recall with increasing fluency inverse facts
- partition numbers into 100s, 10s and 1s or multiple groupings
- understand how the principles of commutative, associative and distributive laws apply or do not apply to multiplication and division
- · understand the effects of scaling by whole numbers and decimal numbers or fractions
- · understand correspondence where n objects are related to m objects
- · investigate and learn rules for divisibility

Herts for Learning Calculation Policy

Progression in addition and subtraction

Addition and subtraction are connected.

Part	Part	
Whole		

Addition names the whole in terms of the parts and **subtraction** names a missing part of the whole.





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Bridging through 10s

This stage encourages children to become more efficient and begin to employ known facts.





7 + 5 is decomposed / partitioned into 7 + 3 + 2. The bead string illustrates 'how many more to the next multiple of 10?' (children should identify how their number bonds are being applied) and then 'if we have used 3 of the 5 to get to 10, how many more do we need to add on? (ability to decompose/partition all numbers applied)

Number track:



Steps can be recorded on a number track alongside the bead string, prior to transition to number line.

Number line



Bead string:



12 - 7 is decomposed / partitioned in 12 - 2 - 5. The bead string illustrates 'from 12 how many to the last/previous multiple of 10?' and then 'if we have used 2 of the 7 we need to subtract, how many more do we need to count back? (ability to decompose/partition all numbers applied)

Number Track:

123456789101121314151617181920

Steps can be recorded on a number track alongside the bead string, prior to transition to number line.

Number Line:



Counting up or 'Shop keepers' method

Bead string:



12 – 7 becomes 7 + 3 + 2.

Starting from 7 on the bead string 'how many more to the next multiple of 10?' (children should recognise how their number bonds are being applied), 'how many more to get to 12?'.

Number Track:



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Bridging with larger numbers

Once secure in partitioning for addition, children begin to explore exchanging. What happens if the ones are greater than 10? Introduce the term 'exchange'. Using the Base 10 equipment, children exchange ten ones for a single tens rod, which is equivalent to crossing the tens boundary on the bead string or number line.







Gradation of difficulty- addition:	Gradation of difficulty- subtraction:		
1. No exchange	1. No exchange		
2. Extra digit in the answer	2. Fewer digits in the answer		
3. Exchanging ones to tens	3. Exchanging tens for ones		
4. Exchanging tens to hundreds	4. Exchanging hundreds for tens		
5. Exchanging ones to tens and tens to hundreds	5. Exchanging hundreds to tens and tens to ones		
6. More than two numbers in calculation	6. As 5 but with different number of digits		
7. As 6 but with different number of digits	7. Decimals up to 2 decimal places (same number of decimal places)		
8. Decimals up to 2 decimal places (same			
number of decimal places)	8. Subtract two or more decimals with a range		
9. Add two or more decimals with a range of decimal places			

Progression in Multiplication and Division

Multiplication and division are connected.

Both express the relationship between a number of equal parts and the whole.

Part	Part	Part	Part
Whole			



The following array, consisting of four columns and three rows, could be used to represent the number sentences: -

3 x 4 = 12,

- 4 x 3 =12,
- 3 + 3 + 3 + 3 = 12,
- 4 + 4 + 4 = 12.

And it is also a model for division

12 ÷ 4 = 3

12 ÷ 3 = 4

12 - 4 - 4 - 4 = 0

12 - 3 - 3 - 3 - 3 = 0

Multiplication	Division
Early experiences Children will have real, practical experiences of handling equal groups of objects and counting in 2s, 10s and 5s. Children work on practical problem solving activities involving equal sets or groups.	Children will understand equal groups and share objects out in play and problem solving. They will count in 2s, 10s and 5s.
10p 10p 10p 10p	
Repeated addition (repeated aggregation)	Sharing equally
3 times 5 is 5 + 5 + 5 = 15 or 5 lots of 3 or 5 x 3	6 sweets get shared between 2 people. How
Children learn that repeated addition can be	many sweets do they each get? A bottle of fizzy
shown on a number line.	drink shared equally between 4 glasses.
Children learn that repeated addition can be	A A A A A A A A A A A A A A A A A A A
shown on a bead string	
	Grouping or repeated subtraction
Children also learn to partition totals into equal trains using Cuisenaire Rods	2 sweets each?
5 x 3 = 15	

Scaling	Repeated subtraction using a bead string or		
This is an extension of augmentation in addition.	, number line		
except, with multiplication, we increase the	$12 \div 3 = 4$		
quantity by a scale factor not by a fixed amount.	-a -a -a -a		
For example, where you have 3 giant marbles	\sim		
and you swap each one for 5 of your friend's	0 1 2 3 4 5 6 7 8 9 10 11 12		
small marbles, you will end up with 15 marbles.			
This can be written as:			
1 + 1 + 1 = 3 (scaled up by 5 ($5 + 5 + 5 = 15$)	The bead string helps children with interpreting		
	uivision calculations, recognising that $12 \div 5$ can be seen as 'bow many 3s make 122'		
	Cuisenaire Rods also bein children to interpret		
For example, find a ribbon that is 4 times as long	division calculations		
as the blue ribbon.			
5 cm 20 cm			
We should also be aware that if we multiply by a			
number less than 1. this would correspond to a			
scaling that reduces the size of the quantity. For			
example, scaling 3 by a factor of 0.5 would			
reduce it to 1.5, corresponding to $3 \times 0.5 = 1.5$.			
	Grouping involving remainders		
	$13 \div 4 = 3 \text{ r1}$		
	4 4 4		
	0 1 2 3 4 5 6 7 8 7 10 11 12 13		
	Or using a bead string see above		
Commutativity			
Children learn that 3 x 5 has the same total as 5	Children learn that division is not commutative and		
x 3.	link this to subtraction.		
This can also be shown on the number line.			
3 x 5 = 15			
5 x 3 = 15			
5 5 5			
0 1 2 6 4 5 6 7 8 8 10 11 12 13 14 16			
~ ~ ~ ~ ~ ~ ~			
Arravs			
Children learn to model a multiplication	Children learn to model a division calculation using		
calculation using an array. This model supports	an array. This model supports their understanding		
their understanding of commutativity and the	of the development of partitioning and the 'bus		
development of the grid in a written method. It	stop method' in a written method. This model also		
also supports the finding of factors of a number.	connects division to finding fractions of discrete		





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Grid method This written strategy is introduced for the multiplication of TO x O to begin with. It may require column addition methods to calculate the total.	The vertical method- 'chunking' leading toIong divisionSee above for example of how this can bemodelled as an array using place value counters.78 ÷ 3 =	
x 300 40 6 3 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	$ \begin{array}{r} 78 \\ - 30 \\ 48 \\ - 30 \\ 10 \times 3) \\ 18 \\ - 18 \\ - 18 \\ 0 \\ \end{array} $ (6 × 3) So 78 ÷ 3 = 10 + 10 + 6 = 26	

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$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$4 \underbrace{34}_{4 \text{ 736}}$ $4 \underbrace{30 + 4}_{4 \text{ 888}} 4 \underbrace{30 + 4}_{4 \text{ 988}} 4 \underbrace{30 + 4}_{136}$	
Gradation of difficulty (short multiplication)	Gradation of difficulty (short division)	
1. TO x O no exchange	1. TO ÷ O no exchange no remainder	
2. TO x O extra digit in the answer	2. TO ÷ O no exchange with remainder	
3. TO x O with exchange of ones into tens	3. TO ÷ O with exchange no remainder	
4. HTO x O no exchange	4. TO ÷ O with exchange, with remainder	
5. HTO x O with exchange of ones into tens	5. Zero in the quotient e.g. 816 ÷ 4 = 204	
6. HTO x O with exchange of tens into	6. As 1-5 HTO ÷ O	
	7. As 1-5 greater number of digits ÷ O	
and tens into hundreds	8. As 1-5 with a decimal dividend e.g. 7.5 ÷ 5 or 0.12 ÷ 3	
8. As 4-7 but with greater number digits x O	9. Where the divisor is a two digit number	
9. O.t x O no exchange	See below for gradation of difficulty with	
10. O.t with exchange of tenths to ones	remainders	
11. As 9 - 10 but with greater number of digits which may include a range of decimal places x O		
	Dealing with remainders	
	Remainders should be given as integers, but children need to be able to decide what to do after division, such as rounding up or down accordingly. e.g.: I have 62p. How many 8p sweets can I	
	buy?	

	 Apples are packed in boxes of 8. There are 86 apples. How many boxes are needed? Gradation of difficulty for expressing remainders 1. Whole number remainder 2. Remainder expressed as a fraction of the divisor 3. Remainder expressed as a simplified fraction 4. Remainder expressed as a decimal 	
Long multiplication—multiplying by more	Long division —dividing by more than one	
than one digit Children will refer back to grid method by using place value counters or Base 10 equipment with no exchange and using synchronised modelling of written recording as a long multiplication model before moving to TO x TO etc.	 digit Children should be reminded about partitioning numbers into multiples of 10, 100 etc. before recording as either:- 1. Chunking model of long division using Base 10 equipment 2. Sharing model of long division using place value counters See the following pages for exemplification of these methods 	
Chunking model of long division using Base	10 equipment	
This model links strongly to the array representa of the array is unknown and by arranging the Ba discover this unknown. The written method shou children make links. 6	tion; so for the calculation 72 ÷ 6 = ? - one side se 10 equipment to make the array we can Id be written alongside the equipment so that	
Begin with divisors that are between 5 and		
	6 72	
 Make a rectangle where one side is 6 (the number dividing by) – grouping 6 tens 		

Children may benefit from practise to make multiples of tens using the hundreds and tens and tens and ones. 289 ÷ 12			
	12	289	
 Make a rectangle where one side is 12 (the number dividing by) using hundreds and tens 20			
120 + 120			
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Sharing model of long division using place value counters

Starting with the most significant digit. share the hundreds. The writing in brackets is for verbal

1 0 4 532 0 4 0 (4 hundreds used) 4 0 1 3 (13 tens) 0 13 <mark>80</mark> 4 532 <mark>٥</mark>8 J, (4 hundreds used) 4 <mark>°8</mark>0 13 (13 tens) 4 (12 tens used) 12 °80 1 (1 ten left)

Moving to ones, exchange tens to ones means that we now have a total of 12 ones counters (hence the arrow)

Moving to tens - exchanging hundreds for tens means that we now have a total of 13 tens